

## Differentiation - Logs and Exponentials

Differentiate each function with respect to  $x$ .

1)  $y = 4^{4x^4}$

$$\frac{dy}{dx} = x \cdot 4^{4x^4+2} \ln 4$$

2)  $y = 4^{-5x^3}$

$$\frac{dy}{dx} = \frac{15x^2 \ln 4}{4^{5x^3}}$$

3)  $y = \log_3 3x^2$

4)  $y = \log_2 4x^2$

$$\frac{dy}{dx} = \frac{2}{x \ln 3}$$

5)  $y = \log_3 (3x^5 + 5)^5$

$$\frac{dy}{dx} = \frac{2}{x \ln 2}$$

6)  $y = \log_5 (-5x^3 - 2)^3$

$$\frac{dy}{dx} = \frac{75x^4}{\ln 3 \cdot (3x^5 + 5)}$$

7)  $y = (4x^3 + 2)^3$

$$\frac{dy}{dx} = \frac{-45x^2}{\ln 5 (-5x^3 - 2)}$$

8)  $y = 3^{(x^4+1)^3}$

$$\frac{dy}{dx} = 9x^2 (4x^3 + 2)^2 \cdot 4x^3 \ln 4$$

9)  $y = 3^{\cos 3x^4}$

$$\frac{dy}{dx} = 4x^3 \cdot 3^{(x^4+1)^3+1} \cdot (x^4+1)^2 \ln 3$$

10)  $y = \log_5 \tan 4x^4$

$$\frac{dy}{dx} = -4x^3 \cdot 3^{\cos 3x^4+1} \cdot \sin 3x^4 \cdot \ln 3$$

$$\frac{dy}{dx} = \frac{16x^3 \cdot \sec^2 4x^4}{\tan 4x^4 \cdot \ln 5}$$